Spoiler-free page.

Your first step, of course, is to put the pieces back together. Once you do that, you will have 5 pieces of paper, each with some quote on it, and each conspicuously missing one word.

For example,


A natural next step is to identify each quote, so that you can find the missing word. As you do this, you will likely find the quotes' authors as well. Here is the full list of quotes with their authors and original texts, with missing words bolded:
"Sweet mother, I cannot weave - slender Aphrodite has overcome me with longing for a girl." Sappho (no main text)
"For harmony is a symphony, and symphony is an agreement; but an agreement of disagreements while they disagree there cannot be; you cannot harmonize that which disagrees." - Plato (The Symposium)
"Should any one of the people not know the art of loving, let him read me; and taught by me, on reading my lines, let him love. By art the ships are onward sped by sails and oars; by art are the light chariots, by art is Love, to be guided." - Ovid (Ars Amatoria)
"Majnun appeared, together with his friends, near the tent of his beloved. So far he had only come by night, wrapped in the cloak of darkness, but now he could bear it no longer. His patience was at an end; he had to see her, Layla, for whom his heart was crying out." - Nizami (Layla and Majnun)
"It happened just as I have said now. The Bretons made a lay to tell how Equitan ended his noble life and how much she loved him, that wife." - Marie de France (Equitan)

The flavor text tells you that "a strong wind blew through time" to mix up the papers and you need to "get things back in order", so you should order these texts by the time they were written:

Sappho: alive c. $630-570$ BCE

Plato: alive c. $424-348$ BCE
Ovid: wrote Ars Amatoria 2 CE
Nizami: alive c. 1141-1209 CE
Marie de France: alive c. 1160 to 1215 CE

Now, put the missing words in the same chronological order:
Aphrodite
aGreement
chAriots
wraPped
happEned
Take the diagonal letters, that is, the $1^{\text {st }}$ letter of the $1^{\text {st }}$ word, the $2^{\text {nd }}$ letter of the $2^{\text {nd }}$ word, and so on, to get the answer: AGAPE (the Greek word for "unconditional love").

